The importance of sampling frequency for estimates of wellbeing dynamics

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Abstract

Using a high-frequency panel survey, we examine the sensitivity of estimated self-reported well-being (SWB) dynamics to using monthly, quarterly, and yearly data. This is an important issue if SWB is to be used to evaluate policy. Results from autoregressive models that account for individual-level heterogeneity indicate that the estimated persistence using yearly data is near zero. However, estimated persistence from monthly and quarterly data is substantial. We estimate that persistence to shocks typically lasts around six months and has a net present value of 75–80 per cent of the contemporaneous effect. Estimates are similar for different domains of SWB.

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1 Introduction

Self-reported well-being (SWB) data is often used to estimate changes in a persons well-being over time due to individual adversity, as well as large-scale events, and there are calls to use SWB to evaluate competing policy choices (e.g. Clark, 2018; De Neve et al., 2020; Frijters et al., 2015). However, the literature on the extent and speed of adaptation to events has mostly analysed yearly panel data (e.g. Clark et al., 2008), and there is little evidence on the sensitivity of results to how frequently SWB is measured. Importantly, shocks that appear largely contemporaneous when studied with yearly data (i.e. have low yearly persistence), may actually cause substantial within-year changes. In this study, we explore the extent and duration of SWB dynamics by estimating the monthly, quarterly and yearly persistence of SWB shocks.

Notably, we use a dynamic SWB model rather than one based on observed events. Thus, the dynamics we study subsume all shocks, giving a big-picture perspective of persistence, of which there is little evidence. A recent exception is Piper (2023), who concludes from analyses of yearly data that there is low persistence in SWB and that SWB determinants are mostly contemporaneous. Our results support a different conclusion.

2 The Singapore Life Panel

Our data come from 37 consecutive waves of the Singapore Life Panel (SLP) spanning September 2015 to September 2018. The SLP is a monthly online household panel survey of about 11,000 Singaporeans aged 50 to 70 (see Vaithianathan et al., 2018, for more information on the SLF). Each month, panel members are asked questions about various topics, including their satisfaction with life, our measure of SWB. Our estimation sample is a balanced panel of 3,055 individuals with non-missing life satisfaction responses, providing 113,035 observations.

Life satisfaction is measured with the question, Taking all things together, how satisfied are you with your life as a whole these days? to which respondents could answer on a five-point scale (very dissatisfied to very satisfied). The survey also includes satisfaction questions about social contacts and family life, daily activities and work, income, economic situation, and health.

¹Also see Bottan and Truglia (2011) and Wunder (2012).

3 Life satisfaction dynamics with yearly, quarterly and monthly data

We first estimate persistence with a simple autoregressive model:

$$y_{i,t} = \rho y_{i,t-s} + x'_{i,t}\beta + \varepsilon_{i,t}, \quad i = 1, \dots, N, \quad t = 1, \dots, T,$$
 (1)

where $y_{i,t}$ denotes the life satisfaction of individual i in month t. To understand the overall persistence in life satisfaction, we include only a parsimonious set of exogenous variables in $x_{i,t}$: indicators for gender, age in years, and year of survey.

We use two approaches to examine the importance of sampling frequency on ρ . First, we include all available monthly observations and vary the lag length (monthly s=1, quarterly s=3, and yearly s=12). Second, we mimic lower-frequency panel data sets by constructing artificial panels: quarterly panel includes December, March, June, and September responses, and yearly panel includes December responses.

Table 1 presents estimates of ρ for different frequencies. The estimates are similar across columns, ranging from 0.728 (yearly panel) to 0.808 (monthly panel), indicating a high period-to-period persistence regardless of the sampling frequency. An autoregressive parameter of 0.8, for example, implies that a one-unit shock in period t will have died away (arbitrarily defined as magnitude < 0.05) within 14 years for the yearly panel and 14 months for the monthly panel. This highlights the speciousness of similar persistence estimates across different frequencies.²

4 Sources of persistence: unobserved heterogeneity vs state dependence

The large persistence estimates in Table 1 indicate that high life satisfaction today predicts high life satisfaction levels in the future. We next establish how much of the variation in estimates is driven by persistence across time within individuals (i.e. state dependence) and time-invariant differences between individuals (i.e. unobserved heterogeneity). To do so, we augment equation (1) with an individual-specific, time-invariant component:

²Selective attrition does not drive these results. Appendix Table A1 reports estimates using the unbalanced sample, and estimates are very similar to those in Table 1.

$$y_{i,t} = \rho y_{i,t-s} + x_{i,t} + \alpha_i + \varepsilon_{i,t}. \tag{2}$$

 ρ now captures the average persistence in life satisfaction within an individual.

It is well-known that the fixed-effects estimator is inconsistent for linear dynamic models Anderson and Hsiao (1981), so we use the split-panel jackknife estimator of Dhaene and Jochmans (2015). If one considers T to be fixed, this estimator is asymptotically equivalent to the GMM estimators of Arellano and Bond (1991) and Blundell and Bond (1998). However, moderately long panels such as the SLP are better described by asymptotics in which T is not fixed. Under these conditions the jackknife estimator is asymptotically efficient (Dhaene and Jochmans, 2015).

Table 2 contains yearly, quarterly, and monthly persistence estimates from the naïve estimator (which suffers from Nickell bias) and the bias-corrected estimator.³ Yearly persistence estimates are near-zero, indicating the Table 1 estimate was driven by time-invariant differences between individuals. In contrast, only roughly 50% of quarterly and monthly persistence are due to time-invariant differences. Thus, leveraging the higher sampling frequency makes it possible to detect substantial within-year dynamic movements in life satisfaction. We next examine this within-year adaptation process.

5 High-frequency estimates of the response to a shock

The monthly estimate (0.436) from Table 2 represents the most finely estimated autoregressive parameter from our data. We use it to trace the adaptation path of a Δ -sized shock to life satisfaction in Figure 1. The red line shows how the shock persists over the next 12 months: $\rho\Delta$ after one month, $\rho^2\Delta$ remains after two months, etc. After six months, the effect is close to zero.

Model (2) is highly stylised, with dynamics represented by a single parameter. While this has parsimony advantages, we can use a less parametric approach by specifying an AR(12) model:

$$y_{i,t} = \sum_{s=1}^{12} \rho_s y_{i,t-s} + x_{i,t} + \alpha_i + \varepsilon_{i,t},$$
 (3)

where the persistence is estimated flexibly via the twelve parameters (ρ_1 to ρ_{12}).

The blue line in Figure 1 shows the estimated adaptation path from the AR(12).⁴ Compared to the AR(1), the AR(12) gives a flatter adaptation trajectory. The immediate depreciation of the life satisfaction shock is larger, with only 25% left after one month. However, the shock persists for longer

³Table 2 highlights the importance of Nickel biases, with bias-corrected estimates substantially larger than naïve ones.

⁴AR(12) estimates are reported in Appendix Table A2.

than the AR(1) implied, disappearing after nine months.

The simple AR(1) appears to be effective at uncovering the presence of persistence. However, the adaptation path may be different than implied by an AR(1). An important metric to assess such differences is net present value (NPV). I.e., the difference in future SWB an individual receives from an initial Δ . Using standard discount rates (e.g. Baetschmann, Staub and Studer, 2016), we find that NPV estimates are similar for both models (see Table 3), varying between 81.5% and 75.0% of the initial shock. However, the NPV for the quarterly AR(1) model is substantially smaller, with values of only 44%-48%. Therefore, the results again indicate that a higher sampling frequency helps detect within-year dynamic movements in life satisfaction.⁵

6 Dynamics in life satisfaction domains

Finally, we explore the dynamics of satisfaction with different domains of life to determine whether particular domains drive the persistence observed above. Specifically, we estimate yearly autoregressive models without fixed effects for each domain, as in equation (1), and yearly, quarterly, and monthly models with fixed effects, as in equation (2). The dynamics for each domain are similar to the dynamics of overall life satisfaction (see Table 4). The largest monthly persistence estimate occurs for income shocks (0.316), and the smallest occurs for social shocks (0.258). Thus, we find little evidence of the differential contribution of satisfaction domains to the persistence of life satisfaction.

7 Discussion

This paper demonstrates the existence of substantial short-term dynamics in life satisfaction. These dynamics add 75–80 percent to the net present worth of a life satisfaction shock and are also present in important domains of life.

This persistence cannot be detected by yearly frequency data that most life satisfaction research relies upon. Therefore, researchers working with such data should be aware that estimated effects on life satisfaction may overlook substantial short-term dynamics, which is an important consideration if SWB measures are to be used to evaluate policies. Quarterly data also significantly underestimates the degree of persistence, but it can be useful for testing the presence of persistence.

⁵While the additional effect of monthly persistence is substantial, it is likely an underestimate of the NPV that could theoretically be obtained with satisfaction measured in continuous time.

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Tables and figures

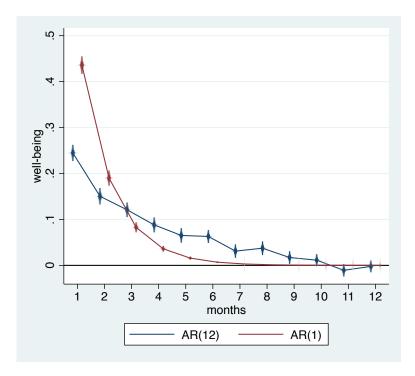


Figure 1: Impulse response plot of two dynamic life satisfaction models with monthly data

Note: The blue line connects the twelve estimated autoregressive coefficients of the AR(12) model (equation 3) estimated by split-panel jackknife; the red line connects estimates obtained from the AR(1) model from Table 2 Column (6) as $\hat{\rho}$, $\hat{\rho}^2$, $\hat{\rho}^3$, etc. for months 1, 2, 3, etc. Control variables: see Table 1 notes. Vertical lines indicate 99% confidence intervals based on robust standard errors clustered at individual level. See Appendix Table A2 for estimates and standard errors for this figure.

Table 1: DYNAMIC MODELS OF LIFE SATISFACTION: POOLED OLS ESTIMATES

	(1)	(2)	(3)	(4)	(5)
	yearly	yearly	quarterly	quarterly	$_{ m monthly}$
lagged life satisfaction	0.728***	0.771***	0.786***	0.792***	0.808***
	(0.009)	(0.011)	(0.006)	(0.007)	(0.005)
N	76,375	6,110	10,3870	33,605	109,980

Notes: Pooled OLS estimates of the autoregressive coefficient in AR(1) models. Control variables: complete sets of year and age (in years) fixed effects, gender dummy. Robust standard errors clustered at individual level in parentheses. Statistical significance: * p < 0.05, *** p < 0.01, **** p < 0.001

Table 2: Dynamic models of life satisfaction: FE and bias-corrected FE estimates

	(1) yearly	(2) yearly bc	(3) quarterly	(4) quart., bc	(5) monthly	(6) monthly, bc
lagged life satisfaction	0.003	0.004	0.195***	0.328***	0.301***	0.436***
	(0.006)	(0.006)	(0.008)	(0.008)	(0.007)	(0.007)
N	76375	76375	103870	103870	109980	109980

Notes: Within estimates (columns 1, 3, 5) and split-panel jackknife estimates (columns 2, 4, 6) of the autoregressive coefficient in AR(1) models with individual-specific fixed effects. Control variables, standard errors and significance: see Table 1 notes.

Table 3: Dynamic models of life satisfaction: Net present value of lagged satisfaction

	Annual discount factor (κ)				
	$\kappa = 1$	κ =0.95	$\kappa = 0.90$	$\kappa = 0.80$	
monthly AR(12) model, fe bc	0.815	0.804	0.794	0.773	
monthly AR(1) model, fe bc	0.773	0.767	0.762	0.750	
quarterly AR(1) model, fe bc	0.482	0.474	0.465	0.448	

Notes: Estimates calculated based on Cols (2) [monthly AR(12) model] and (3) [monthly AR(1) model] of Table A2, and (monthly prorated) annual discount factors κ . Quarterly AR(1) model estimates based on Table 2 Col (4) and quarterly prorated factors.

Table 4: Dynamic models of domain satisfaction: Pooled and Bias-Corrected FE estimates

	(1)	(2)	(3)	(4)
	pooled year	bc fe year	bc fe quart	bc fe month
lagged satisfaction with family	0.727***	0.004	0.167***	0.258***
	(0.009)	(0.005)	(0.007)	(0.007)
N	76332	76332	103816	109921
lagged satisfaction with income	0.772***	-0.008	0.208***	0.316***
	(0.007)	(0.006)	(0.008)	(0.008)
N	76322	76322	103803	109908
lagged satisfaction w. econ. situation	0.764***	-0.010	0.173***	0.281***
	(0.007)	(0.005)	(0.007)	(0.007)
N	76315	76315	103786	109890
lagged satisfaction with health	0.762***	0.000	0.158***	0.277***
	(0.008)	(0.005)	(0.007)	(0.007)
N	76341	76341	103822	109930
lagged satisfaction with job	0.710***	-0.001	0.166***	0.268***
	(0.009)	(0.005)	(0.007)	(0.007)
N	76288	76288	103760	109865

Notes: Each panel depicts the autoregressive coefficient in a separate AR(1) model with dependent variables each of the five satisfaction domains-family, income, etc. Cols. (1)-(2) include a yearly lag, (3) a quarterly lag, (4) a monthly lag. Control variables, standard errors and significance: see Table 1 notes.

Additional tables for online appendix

Table A1: Dynamic models of life satisfaction: Pooled OLS estimates, unbalanced samples

	(1)	(2)	(3)	(4)	(5)
	yearly	yearly	quarterly	quarterly	$_{ m monthly}$
lagged life satisfaction	0.689***	0.729***	0.755***	0.759***	0.785***
	(0.006)	(0.008)	(0.004)	(0.005)	(0.004)
N	184332	15246	251362	80332	263563

Notes: Pooled OLS estimates of the autoregressive coefficient in AR(1) models. of Control variables, standard errors and significance: see Table 1 notes.

Table A2: Dynamic models of life satisfaction: AR(12) models with monthly data

	(1)	(2)	(3)
	fe	fe, bc	fe, bc, based on $ar(1)$
Life satisfaction, 1st lag	0.156***	0.245***	0.436***
	(0.007)	(0.007)	(0.007)
Life satisfaction, 2nd lag	0.078***	0.150***	0.190***
	(0.007)	(0.007)	(0.006)
Life satisfaction, 3rd lag	0.059***	0.121***	0.083***
	(0.006)	(0.006)	(0.004)
Life satisfaction, 4th lag	0.035***	0.088***	0.036***
	(0.006)	(0.006)	(0.002)
Life satisfaction, 5th lag	0.020**	0.065***	0.016***
	(0.006)	(0.006)	(0.001)
Life satisfaction, 6th lag	0.024***	0.063***	0.007***
	(0.006)	(0.006)	(0.001)
Life satisfaction, 7th lag	0.000	0.031***	0.003***
	(0.006)	(0.006)	(0.000)
Life satisfaction, 8th lag	0.012*	0.037***	0.001***
	(0.006)	(0.006)	(0.000)
Life satisfaction, 9th lag	-0.003	0.017**	0.001***
	(0.005)	(0.005)	(0.000)
Life satisfaction, 10th lag	-0.000	0.011*	0.000***
	(0.005)	(0.005)	(0.000)
Life satisfaction, 11th lag	-0.015**	-0.011*	0.000***
	(0.005)	(0.005)	(0.000)
Life satisfaction, 12th lag	0.000	-0.002	0.000***
	(0.005)	(0.005)	(0.000)
N	76375	76375	76375

Note: Estimates of the autoregressive coefficients in AR(12) models (Cols. 1–2) and AR(1) models (Col. 3). Col. (1) obtained using the within estimator, Cols. (2) and (3) using the split-panel jackknife estimator. Estimates of the autoregressive coefficients of order higher than 1 in Col. (3) obtained as powers of $\hat{\rho}$: $\hat{\rho}^2$, $\hat{\rho}^3$, etc. for second lag, third lag, etc. Standard errors for Col. (3) based on Delta method. Estimates from Cols. (2) and (3) are plotted in Fig. 1. Control variables, standard errors and significance: see Table 1 notes.